**Programming Project 1:**

**Solving the 8-puzzle using A\* algorithm**

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The program applies A\* algorithm to solve any N-puzzle problem. Dimensions of the boarding game are specified in Main.java ln: 12 and can be easily changed to any other N-puzzle problem. The program accept any initial and goal state and determines if it is solvable. If yes it prints out the states the algorithm takes to go from initial state to goal state, alongside number of total nodes generated in search tree and number of expanded nodes.

Number of expanded nodes is actually the same as number of states that should be visited during the algorithm and is saved in a variable called numberOfMoves in the code.

Number of total generated nodes is equal to size of the PriorityQueue that stores all of the SreachNodes created. After finding the goal state since every SearchNode keeps track of its previous node, we can chase the nodes all the way back to initial state. That’s how the program outputs the path.

What is 8 puzzle?  
Given a 3×3 board with 8 tiles (every tile has one number from 1 to 8) and one empty space. The objective is to place the numbers on tiles in an arbitrary order given as goal state. We can slide four adjacent (left, right, above and below) tiles into the empty space.

**Goal Formulation:** Goal is described as an order of numbers that should be displayed on the board.

**Search Algorithm:** A\*

**Problem Formulation:**

*Initial State:* From Input

*Goal State:* From Input

*Possible Actions:* Left, Right, Above, Below

*State Space:* 3\*3 board

*Path:* Different states of the board during the execution time

*Path cost:* Number of moves prior to this state used as g(n) in algorithm to set the priority of searchNodes in the PriorityQueue.

Heuristic Function:

h1 (n) = number of misplaced tiles

h2 (n) = total Manhattan distance

Since h1 dominates h2, it is better for search and has a smaller branching factor. This function is used in this implementation of A\*.

The program starts from Main.java and after creating the initial State by calling its class constructor, it calls the solve(state) method of AStar class which returns the number of nodes generated and stores the path from initial to goal state.

In AStar class the program uses java.util.Stack class to store all the states (expanded nodes) and all the SearchNodes (generated nodes) are stored in a priorityQueue called queue.

Here I used the fact that “exactly one of a board and its twin are solvable” to determine whether a puzzle is solvable or not, where “A twin is obtained by swapping two adjacent blocks (the blank does not count) in the same row”. <http://coursera.cs.princeton.edu/>

State class represents the board in each step of the algorithm. It keeps the position of all 8 numbers in a 3\*3 array called Tiles. Following methods are implemented in this class:

* manhatan() *sum of Manhattan distances between tiles and goal State*
* twin()  *Returns a new Board result of swapping to adjacent tiles*
* neighbors() returns the neighbors of each state/node

## Execution Instruction:

Run the program from command line. First, compile AStar.java State.java and Main.java using command “javac Astar.java”. Next, execute Main and pass the initial and goal states as parameters, separate tiles by space (also use space to separate initial form goal states)

Example:

Initial state: 5 4 0

6 1 8

7 3 2

Goal State: 1 2 3

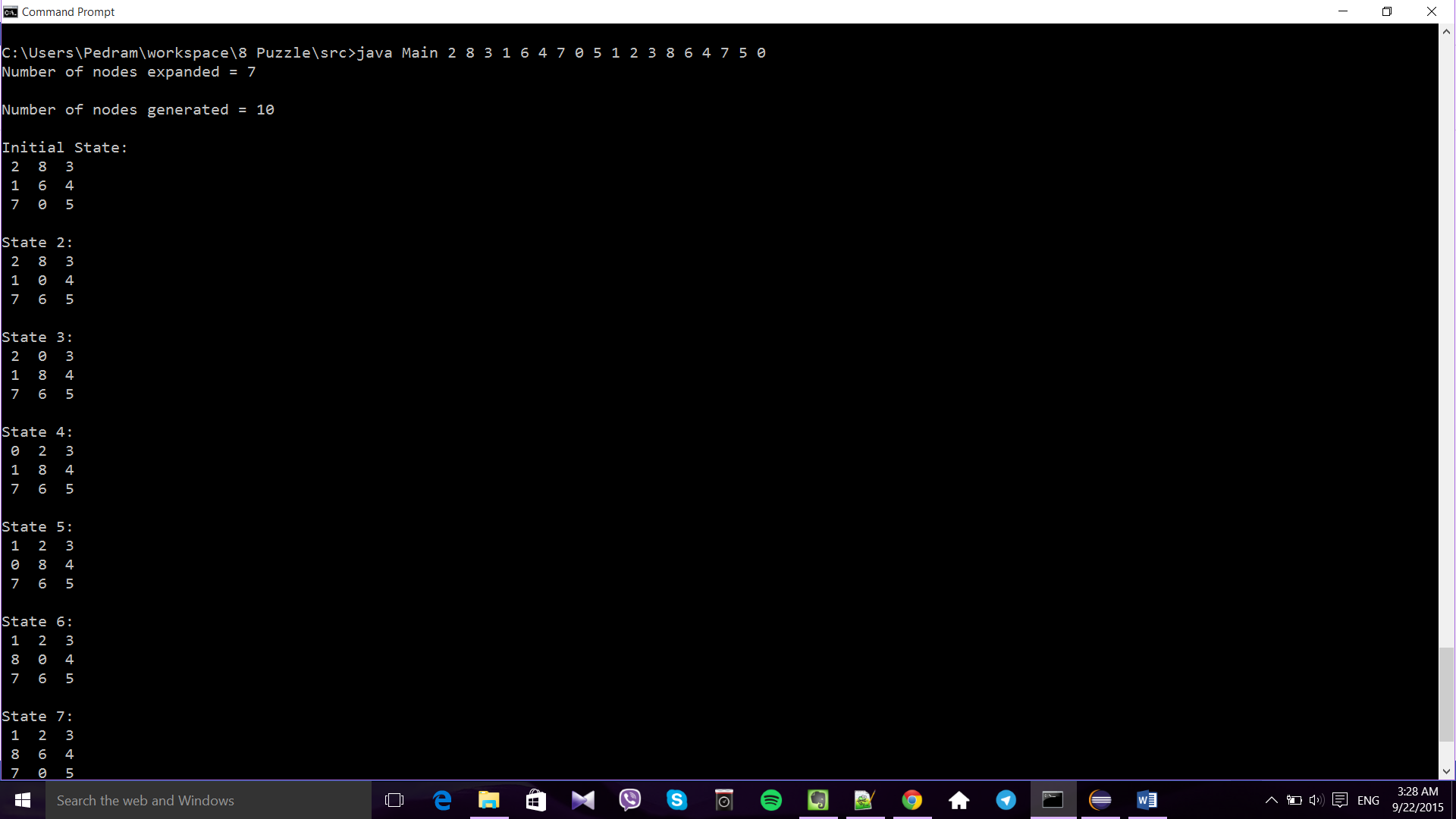
4 0 5

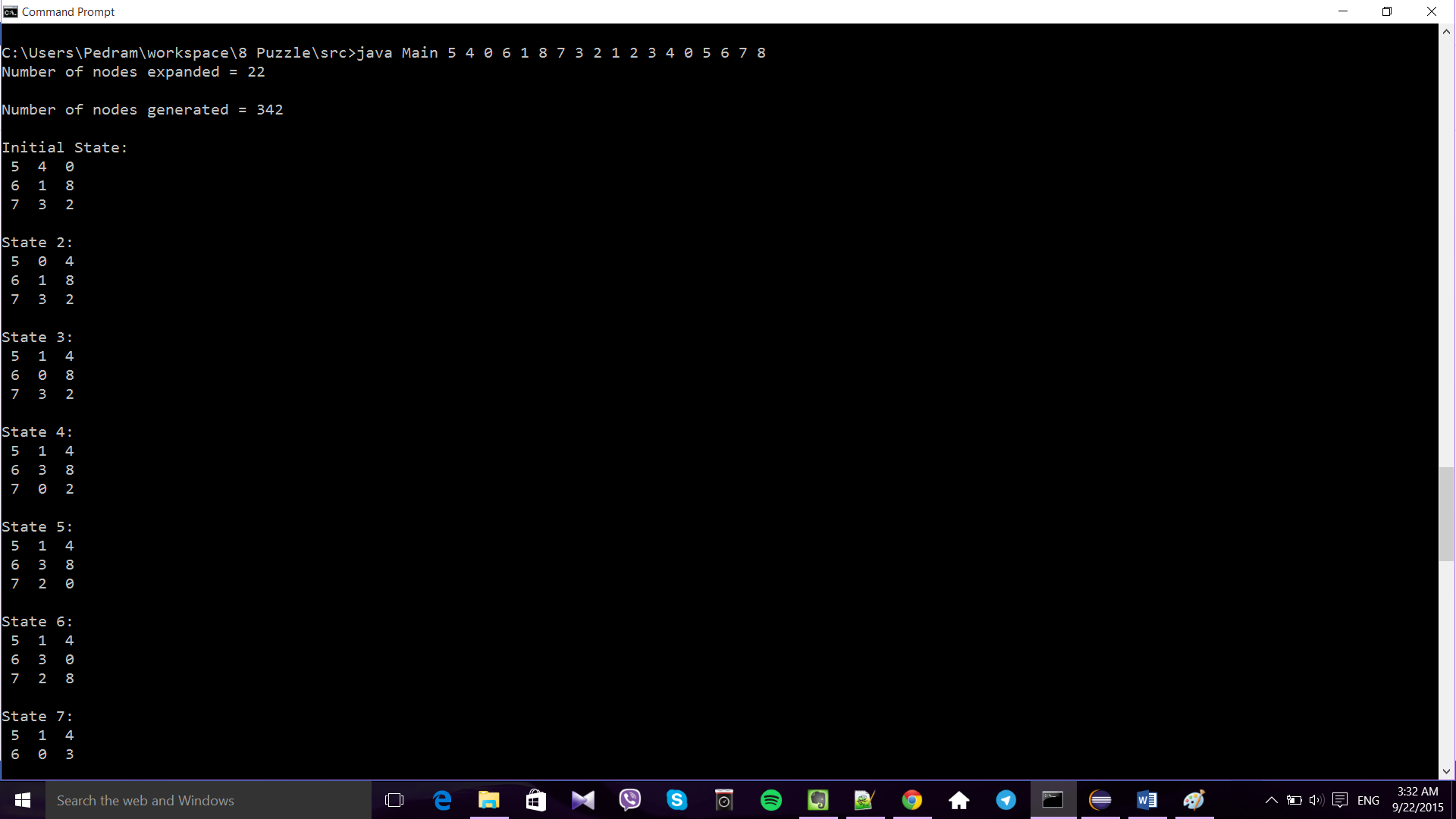
6 7 8

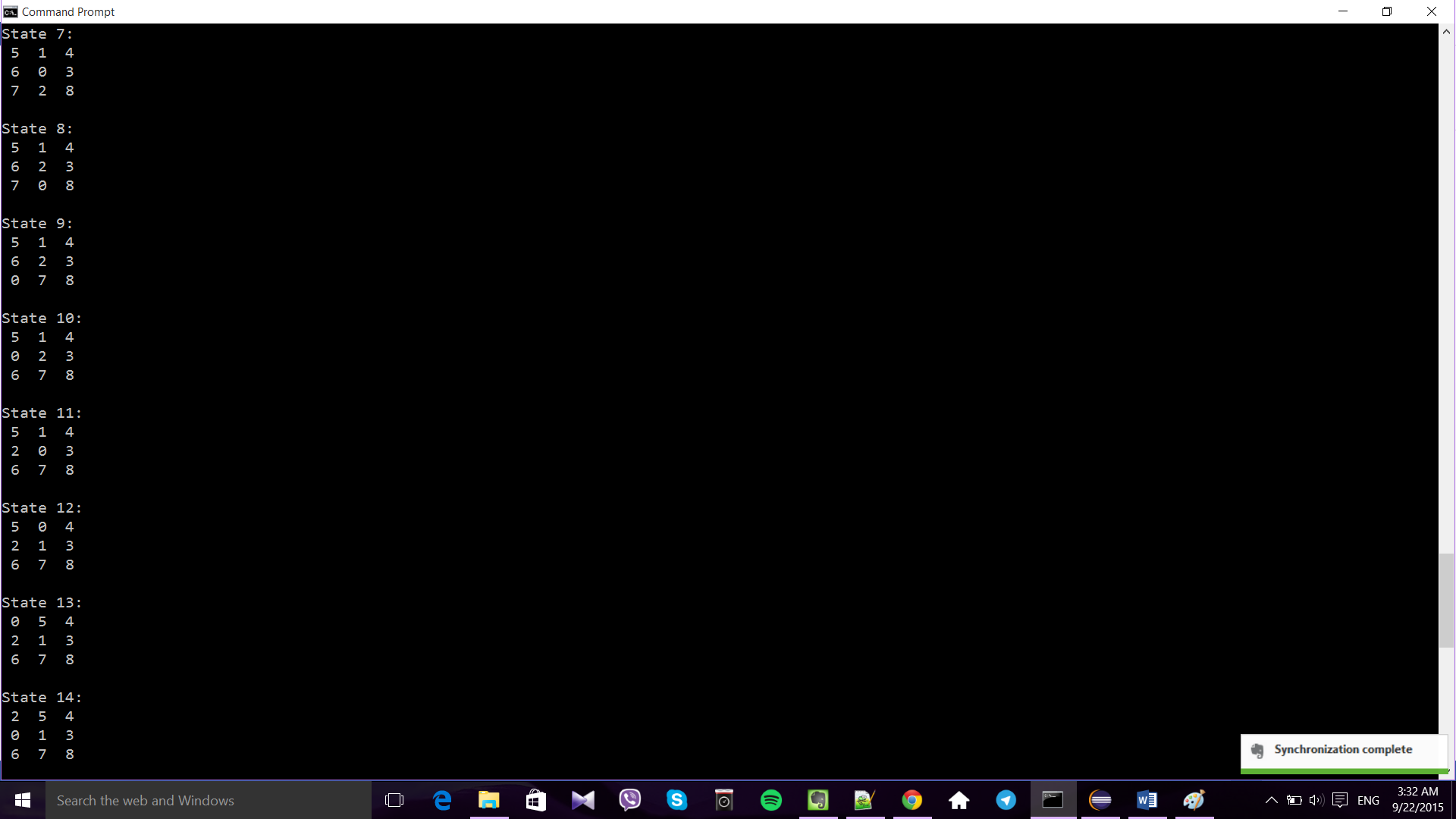
Command should be like:

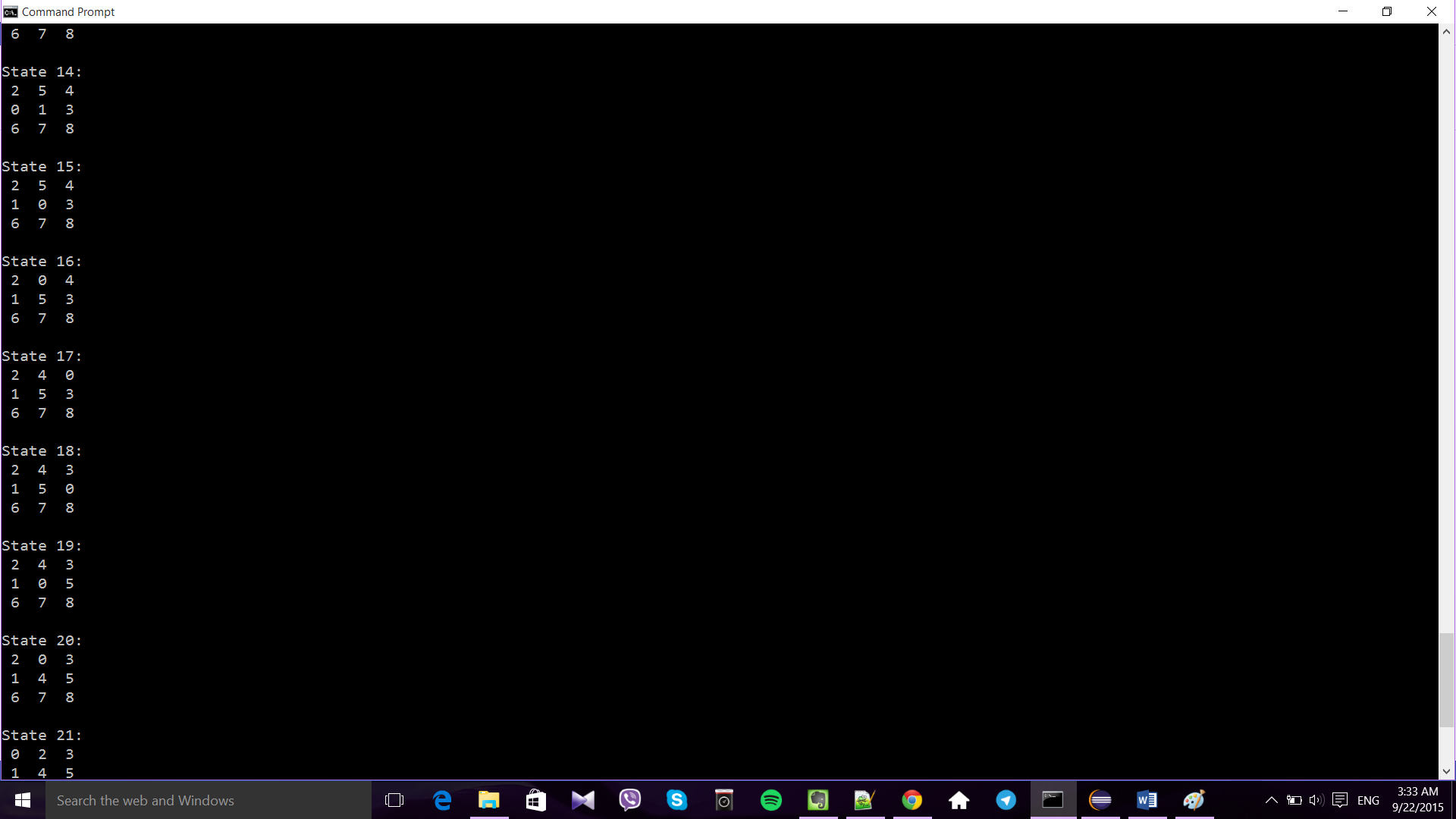
“java Main 5 4 0 6 1 8 7 3 2 1 2 3 4 0 5 6 7 8”

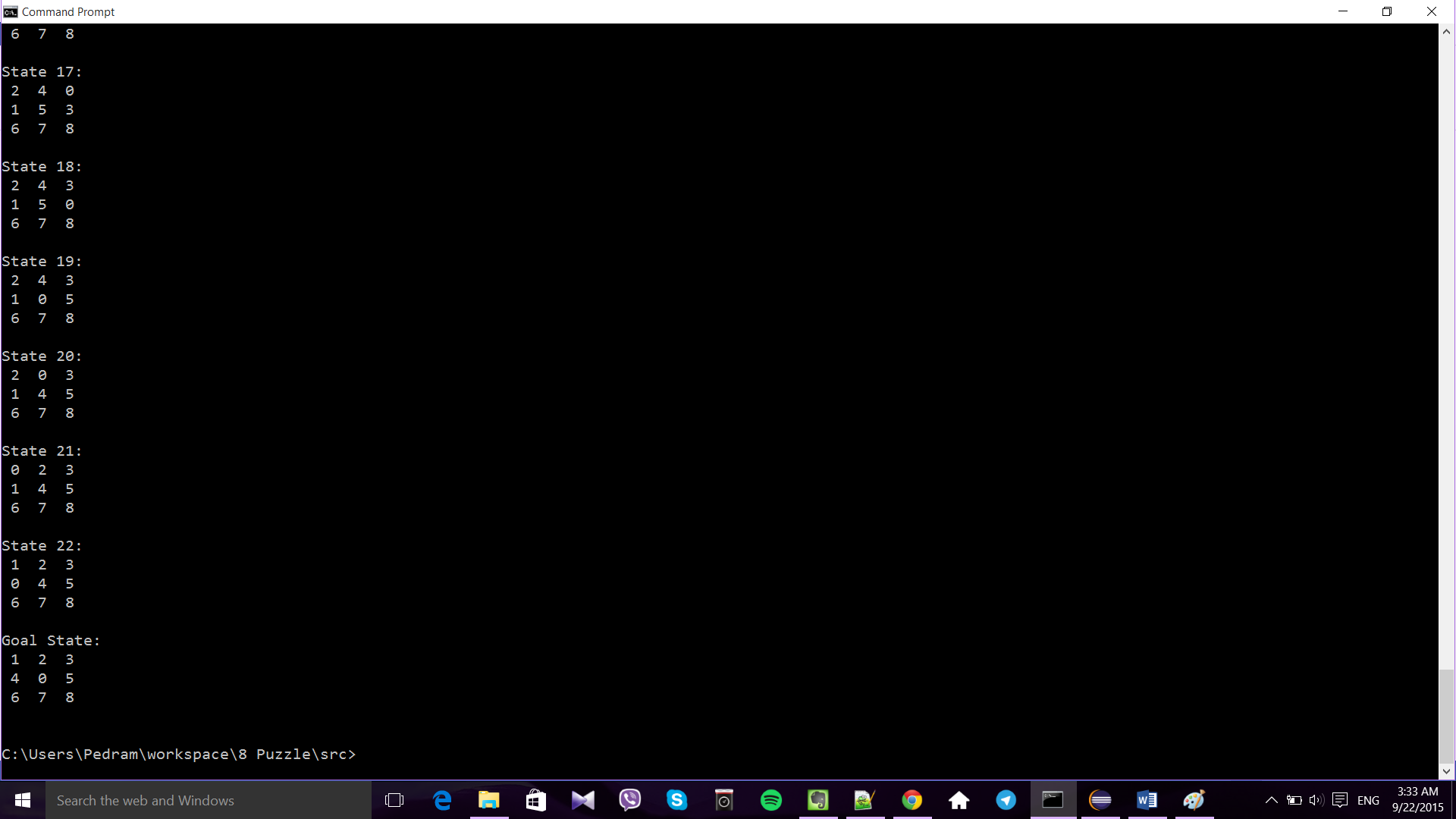
## The execution results for some example pairs:

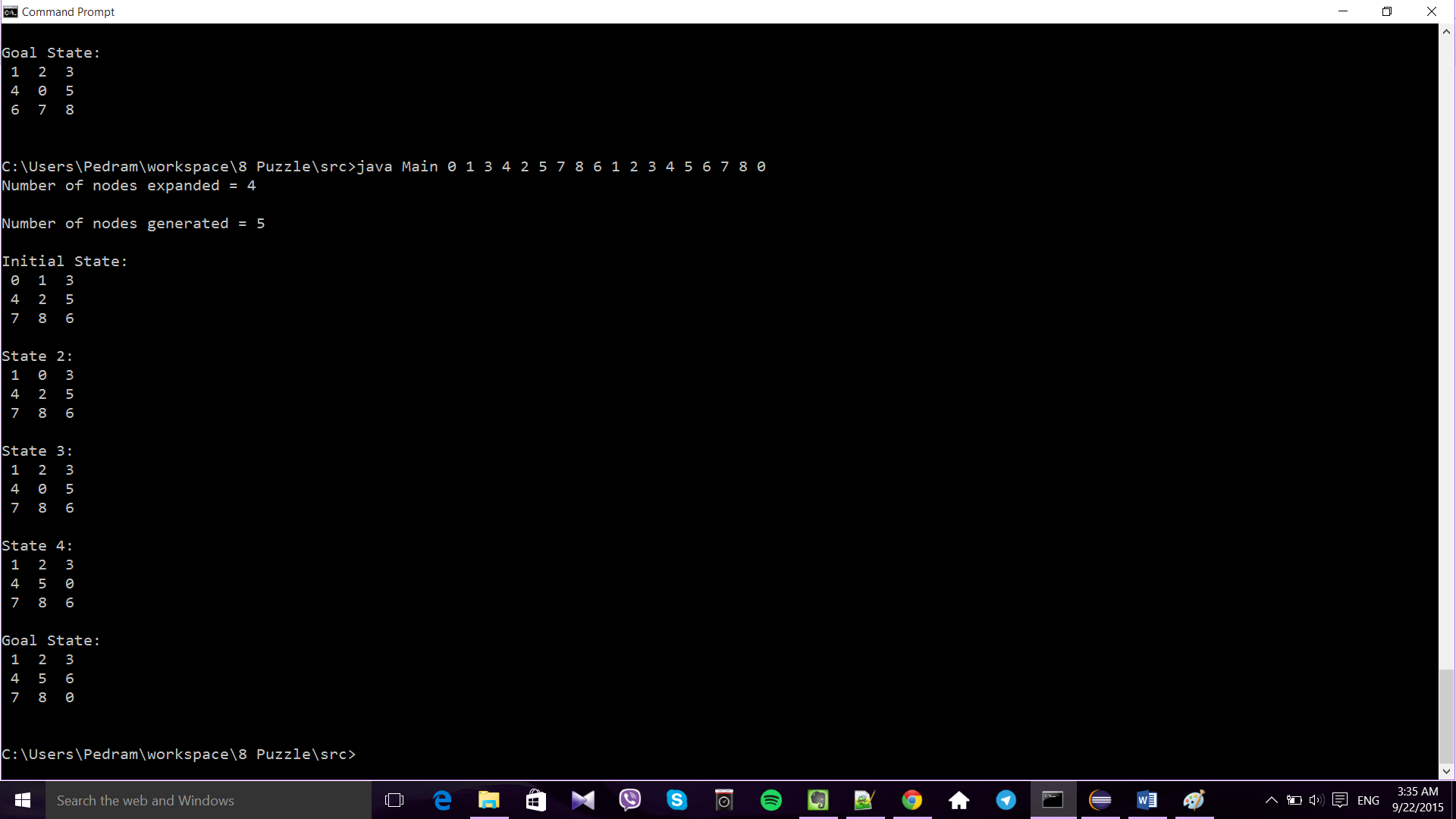












## Source Code

**Main.java:**

import java.util.Collections;

import java.util.List;

public class Main {

public static void main(String[] args) {

AStar Solver = new AStar();

int count = 0;

int n = 3;

// Get Initial State form input

int[][] initialState = new int[n][n];

for (int i = 0; i < n; i++) {

for (int j = 0; j < n; j++) {

initialState[i][j] = Integer.parseInt(args[count]);

count++;

}

}

// Initialize the board

State initial = new State(initialState);

// Get Final State from input

Solver.finalState = new int[n][n];

for (int i = 0; i < n; i++) {

for (int j = 0; j < n; j++) {

Solver.finalState[i][j] = Integer.parseInt(args[count]);

count++;

}

}

// solve the puzzle

int nodesGenerated = Solver.solve(initial);

// print solution to standard output

if (!Solver.isSolvable())

System.out.println("Unsolvable");

else {

System.out.println("Number of nodes expanded = "

+ Solver.numberOfMoves() + "\n");

System.out.println("Number of nodes generated = " + nodesGenerated

+ "\n");

Iterable<State> result = Solver.solution();

List<State> resultList = (List<State>) result;

if (result != null) {

Collections.reverse(resultList);

int counter = 0;

System.out.println("Initial State:");

for (State board : resultList) {

if (counter == 0)

counter++;

else if (counter == resultList.size() - 1)

System.out.println("Goal State" + ":");

else

System.out.println("State " + ++counter + ":");

System.out.println(board);

}

}

}

}

}

**AStar.java:**

import java.util.PriorityQueue;

import java.util.Stack;

public class AStar {

private boolean isSolvable;

public int[][] finalState;

private int numberOfMoves;

private final Stack<State> states;

private class SearchNode implements Comparable<SearchNode> {

private State state;

private int moves;

private SearchNode previous;

private int cachedPriority = -1;

SearchNode(State state, int moves, SearchNode previous) {

this.state = state;

this.moves = moves;

this.previous = previous;

}

private int priority() {

if (cachedPriority == -1) {

cachedPriority = moves + state.manhattan(finalState);

}

return cachedPriority;

}

@Override

public int compareTo(SearchNode that) {

if (this.priority() < that.priority()) {

return -1;

}

if (this.priority() > that.priority()) {

return +1;

}

return 0;

}

}

public boolean isSolvable() {

return isSolvable;

}

public int numberOfMoves() {

if (isSolvable) {

return states.size() - 1;

} else {

return -1;

}

}

// Sequence of states from initial to goal state

public Iterable<State> solution() {

if (isSolvable) {

return states;

} else {

return null;

}

}

// Apply A\* algorithm

public int solve(State initial) {

if (initial.isGoalState(finalState)) {

isSolvable = true;

this.states.push(initial);

return 0;

}

if (initial.twin().isGoalState(finalState)) {

isSolvable = false;

return 0;

}

PriorityQueue<SearchNode> queue = new PriorityQueue<SearchNode>();

PriorityQueue<SearchNode> twinQueue = new PriorityQueue<SearchNode>();

numberOfMoves = 0;

State board = initial;

State boardTwin = initial.twin();

SearchNode node = new SearchNode(board, 0, null);

SearchNode nodeTwin = new SearchNode(boardTwin, 0, null);

queue.add(node);

twinQueue.add(nodeTwin);

while (numberOfMoves < 100) {

node = queue.remove();

nodeTwin = twinQueue.remove();

board = node.state;

boardTwin = nodeTwin.state;

// Just one of a board and its twin is solvable

if (boardTwin.isGoalState(finalState)) {

isSolvable = false;

return queue.size();

}

if (board.isGoalState(finalState)) {

isSolvable = true;

this.states.push(board);

while (node.previous != null) {

node = node.previous;

this.states.push(node.state);

}

return queue.size();

}

node.moves++;

nodeTwin.moves++;

Iterable<State> neighbors = board.neighbors();

for (State neighbor : neighbors) {

if (node.previous != null

&& neighbor.equals(node.previous.state)) {

continue;

}

SearchNode newNode = new SearchNode(neighbor, node.moves, node);

queue.add(newNode);

}

Iterable<State> neighborsTwin = boardTwin.neighbors();

for (State neighbor : neighborsTwin) {

if (nodeTwin.previous != null

&& neighbor.equals(nodeTwin.previous.state)) {

continue;

}

SearchNode newNode = new SearchNode(neighbor, nodeTwin.moves,

nodeTwin);

twinQueue.add(newNode);

}

}

return queue.size();

}

public AStar() {

// TODO Auto-generated constructor stub

states = new Stack<State>();

}

}

**State.java:**

import java.util.Stack;

public class State {

private final int N;

private final int[][] Tiles;

public State(int[][] positions) {

N = positions.length;

Tiles = new int[N][N];

for (int i = 0; i < N; i++) {

for (int j = 0; j < N; j++) {

Tiles[i][j] = positions[i][j];

}

}

}

// is this board the goal board?

public boolean isGoalState(int[][] goalState) {

return compare(this.Tiles, goalState);

}

private boolean compare(int[][] first, int[][] second) {

for (int i = 0; i < N; i++) {

for (int j = 0; j < N; j++) {

if (first[i][j] != second[i][j]) {

return false;

}

}

}

return true;

}

// sum of Manhattan distances between tiles and goal State

public int manhattan(int[][] finalState) {

int sum = 0;

for (int i = 0; i < N; i++) {

for (int j = 0; j < N; j++) {

int value = Tiles[i][j];

if (value != 0 && value != finalState[i][j]) {

int distance = Math.abs(i

- getFinalPosition(value, finalState)[0])

+ Math.abs(j

- getFinalPosition(value, finalState)[1]);

sum += distance;

}

}

}

return sum;

}

public int[] getFinalPosition(int valueToSearch, int[][] finalState) {

int[] result = new int[2];

for (int i = 0; i < finalState.length; i++)

for (int j = 0; j < finalState[0].length; j++) {

if (finalState[i][j] == valueToSearch) {

result[0] = i;

result[1] = j;

return result;

}

}

return result;

}

// Returns a new Board result of swapping to adjacent tiles

public State twin() {

State board = new State(Tiles);

for (int i = 0; i < N; i++) {

for (int j = 0; j < N - 1; j++) {

if (Tiles[i][j] != 0 && Tiles[i][j + 1] != 0) {

board.swap(i, j, i, j + 1);

return board;

}

}

}

return board;

}

private boolean swap(int i, int j, int it, int jt) {

if (it < 0 || it >= N || jt < 0 || jt >= N) {

return false;

}

int temp = Tiles[i][j];

Tiles[i][j] = Tiles[it][jt];

Tiles[it][jt] = temp;

return true;

}

// returns neighboring states

public Iterable<State> neighbors() {

int i0 = 0, j0 = 0;

boolean found = false;

for (int i = 0; i < N; i++) {

for (int j = 0; j < N; j++) {

if (Tiles[i][j] == 0) {

i0 = i;

j0 = j;

found = true;

break;

}

}

if (found) {

break;

}

}

Stack<State> boards = new Stack<State>();

State board = new State(Tiles);

boolean isNeighbor = board.swap(i0, j0, i0 - 1, j0);

if (isNeighbor) {

boards.push(board);

}

board = new State(Tiles);

isNeighbor = board.swap(i0, j0, i0, j0 - 1);

if (isNeighbor) {

boards.push(board);

}

board = new State(Tiles);

isNeighbor = board.swap(i0, j0, i0 + 1, j0);

if (isNeighbor) {

boards.push(board);

}

board = new State(Tiles);

isNeighbor = board.swap(i0, j0, i0, j0 + 1);

if (isNeighbor) {

boards.push(board);

}

return boards;

}

@Override

public String toString() {

StringBuilder s = new StringBuilder();

for (int i = 0; i < N; i++) {

for (int j = 0; j < N; j++) {

s.append(String.format("%2d ", Tiles[i][j]));

}

s.append("\n");

}

return s.toString();

}

@Override

public boolean equals(Object x) {

if (x == this)

return true;

if (x == null)

return false;

if (x.getClass() != this.getClass())

return false;

State that = (State) x;

return this.N == that.N && compare(this.Tiles, that.Tiles);

}

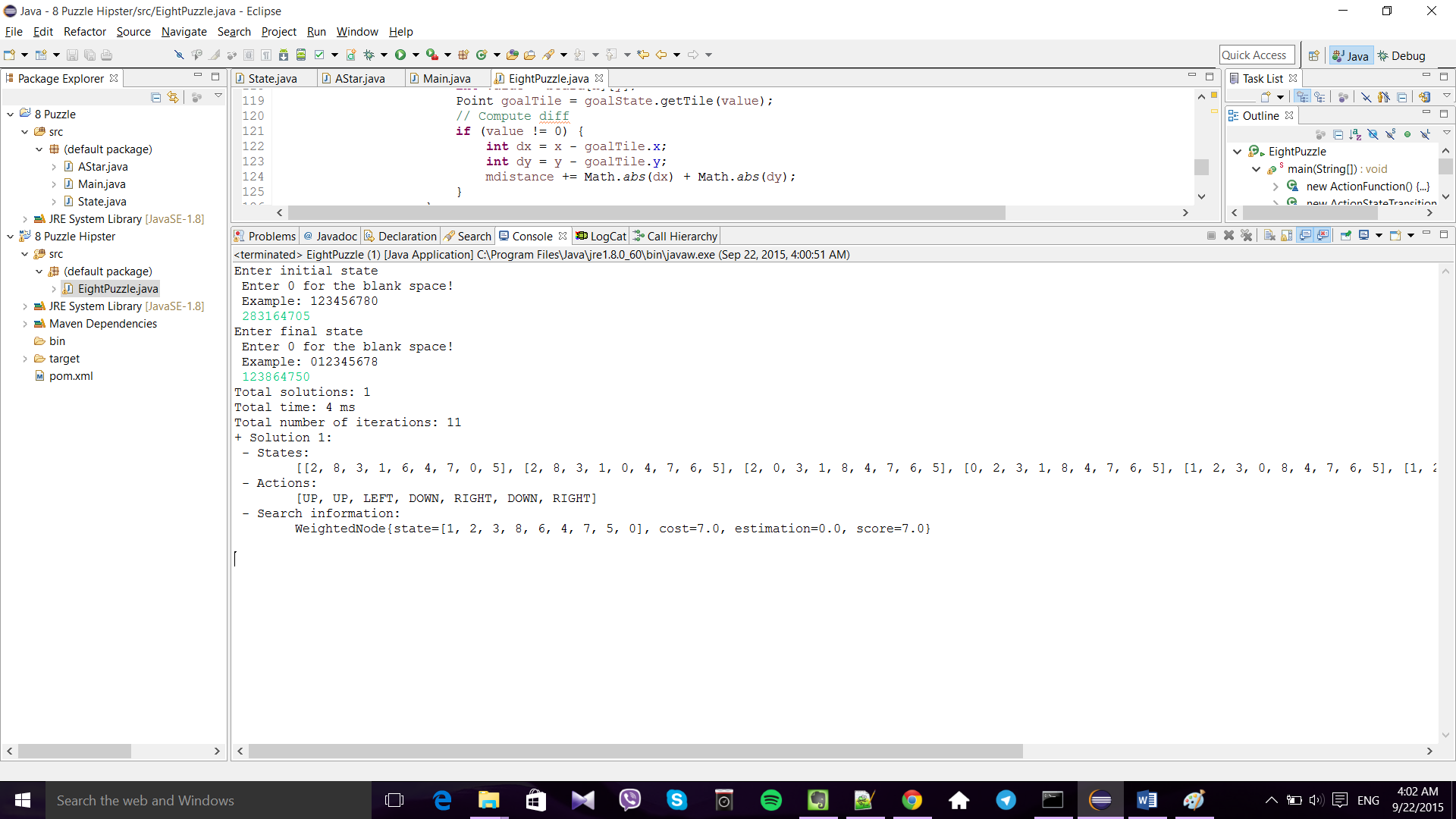
}

# Second Implementation

As I was researching about the subject I came across this interesting library called hipster -An Open Source Java Library for Heuristic Search- which is an easy to use yet powerful library for heuristic search, written in pure Java. <http://www.hipster4j.org/>

Using this library I could easily define the 8 puzzle problem, search strategy and introduce the desired heuristic function. The library solves the problem using A\* with Manhattan distance as the heuristic and returns the path as well as detailed information of the actions, time, and number of iterations.

Below is a result of running the code:



To execute this program the best way is to open the code with eclipse because I have used maven to add the libraries. Compiling maven projects from windows command prompt is not really convenient.

## Source Code:

**EightPuzzle.java:**

import java.awt.Point;

import java.util.LinkedList;

import java.util.Scanner;

import es.usc.citius.hipster.algorithm.Hipster;

import es.usc.citius.hipster.examples.problem.NPuzzle.Puzzle;

import es.usc.citius.hipster.examples.problem.NPuzzle.PuzzleMove;

import es.usc.citius.hipster.model.Transition;

import es.usc.citius.hipster.model.function.ActionFunction;

import es.usc.citius.hipster.model.function.ActionStateTransitionFunction;

import es.usc.citius.hipster.model.function.CostFunction;

import es.usc.citius.hipster.model.function.HeuristicFunction;

import es.usc.citius.hipster.model.impl.WeightedNode;

import es.usc.citius.hipster.model.problem.ProblemBuilder;

import es.usc.citius.hipster.model.problem.SearchProblem;

public class EightPuzzle {

public static void main(String[] args) {

System.out

.print("Enter initial state \n Enter 0 for the blank space! \n Example: 123456780 \n ");

Scanner scan = new Scanner(System.in);

String input = scan.nextLine();

final Puzzle initialState = new Puzzle(new int[] {

input.charAt(0) - 48, input.charAt(1) - 48,

input.charAt(2) - 48, input.charAt(3) - 48,

input.charAt(4) - 48, input.charAt(5) - 48,

input.charAt(6) - 48, input.charAt(7) - 48,

input.charAt(8) - 48 });

System.out

.print("Enter final state \n Enter 0 for the blank space! \n Example: 012345678\n ");

input = scan.nextLine();

final Puzzle goalState = new Puzzle(new int[] { input.charAt(0) - 48,

input.charAt(1) - 48, input.charAt(2) - 48,

input.charAt(3) - 48, input.charAt(4) - 48,

input.charAt(5) - 48, input.charAt(6) - 48,

input.charAt(7) - 48, input.charAt(8) - 48 });

// ActionFunction: Taking an state as input, determine the actions which

// can be applied to reach other state.

ActionFunction<PuzzleMove, Puzzle> af = new ActionFunction<PuzzleMove, Puzzle>() {

@Override

public Iterable<PuzzleMove> actionsFor(Puzzle state) {

LinkedList<PuzzleMove> movements = new LinkedList<PuzzleMove>();

// Get which place the gap tile is in

Point gap = state.getTile(0);

// side size of the board

int boardSize = state.getMatrixBoard().length;

// Check valid movements. There are always maximum

// 4 tiles around the gap (left, right, top, down)

if (gap.getX() > 0 && gap.getX() < boardSize) {

movements.add(PuzzleMove.UP);

}

if (gap.getX() >= 0 && gap.getX() < boardSize - 1) {

movements.add(PuzzleMove.DOWN);

}

if (gap.getY() >= 0 && gap.getY() < boardSize - 1) {

movements.add(PuzzleMove.RIGHT);

}

if (gap.getY() > 0 && gap.getY() < boardSize) {

movements.add(PuzzleMove.LEFT);

}

return movements;

}

};

// ActionStateTransitionFunction: Taking as input the current state and

// current action. It generates following state after applying the

// action.

ActionStateTransitionFunction<PuzzleMove, Puzzle> atf = new ActionStateTransitionFunction<PuzzleMove, Puzzle>() {

@Override

public Puzzle apply(PuzzleMove action, Puzzle state) {

// Generate the next board

Point gap = state.getTile(0);

int[][] board = state.copyBoard();

// System.out.println("Applying " + action + " to " + state +

// " gap: " + gap.toString());

// x=row, y=column

switch (action) {

case UP:

board[gap.x][gap.y] = state.getMatrixBoard()[gap.x - 1][gap.y];

board[gap.x - 1][gap.y] = 0;

break;

case DOWN:

board[gap.x][gap.y] = state.getMatrixBoard()[gap.x + 1][gap.y];

board[gap.x + 1][gap.y] = 0;

break;

case LEFT:

board[gap.x][gap.y] = state.getMatrixBoard()[gap.x][gap.y - 1];

board[gap.x][gap.y - 1] = 0;

break;

case RIGHT:

board[gap.x][gap.y] = state.getMatrixBoard()[gap.x][gap.y + 1];

board[gap.x][gap.y + 1] = 0;

break;

}

Puzzle successor = new Puzzle(board);

return successor;

}

};

// definition of an uniform cost function g(n)

CostFunction<PuzzleMove, Puzzle, Double> cf = new CostFunction<PuzzleMove, Puzzle, Double>() {

@Override

public Double evaluate(Transition<PuzzleMove, Puzzle> transition) {

return 1d;

}

};

// definition of an heuristic, the Manhattan distance between states

// h(n)

HeuristicFunction<Puzzle, Double> hf = new HeuristicFunction<Puzzle, Double>() {

@Override

public Double estimate(Puzzle state) {

// Compute the manhattan distance

int mdistance = 0;

int[][] board = state.getMatrixBoard();

int size = board.length;

for (int x = 0; x < size; x++)

for (int y = 0; y < size; y++) {

int value = board[x][y];

Point goalTile = goalState.getTile(value);

// Compute diff

if (value != 0) {

int dx = x - goalTile.x;

int dy = y - goalTile.y;

mdistance += Math.abs(dx) + Math.abs(dy);

}

}

return (double) mdistance;

}

};

/\*

\* Search problem is instantiated defining all the components to be used

\* in the search: the initial state,the action and transition function,

\* and the cost and heuristic SO let's formulate the problme.

\*/

SearchProblem<PuzzleMove, Puzzle, WeightedNode<PuzzleMove, Puzzle, Double>> p = ProblemBuilder

.create().initialState(initialState)

.defineProblemWithExplicitActions().useActionFunction(af)

.useTransitionFunction(atf).useCostFunction(cf)

.useHeuristicFunction(hf).build();

// Here we assign A\* as the search algorithm

// search() method starts the search process until the goal state is

// reached

// and print out time, number of iterations, and cost of the search .

System.out.println(Hipster.createAStar(p).search(goalState));

}

}